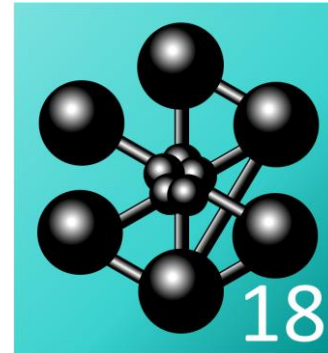


DE LA RECHERCHE À L'INDUSTRIE

cea

PARIS-SACLAY



# ANALYSE MULTI-ÉCHELLE DE CÂBLES SUPRACONDUCTEURS

G. Lenoir, P. Manil, F. Nunio

CEA Paris-Saclay – IRFU, Université Paris-Saclay

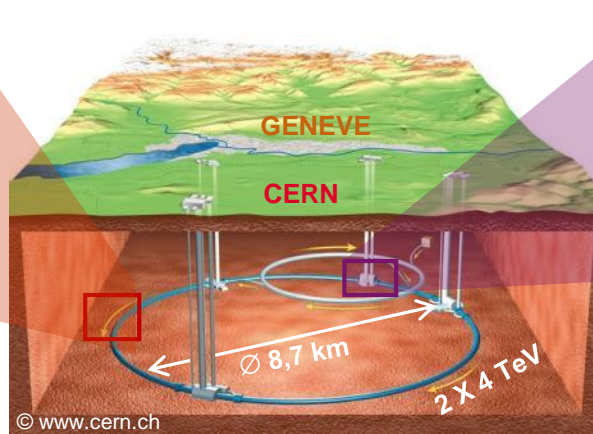
Club Cast3m 2018 - Paris

04/02/2019



Circular particle accelerators magnet :

Dipole & Quadrupole LHC (NbTi) →  $B_{max} < 9T$



© www.cern.ch



Detector magnet :

ATLAS (NbTi) →  $B_{max} < 4T$

Principle of a circular accelerator, to ensure the collision of the 2 beams :

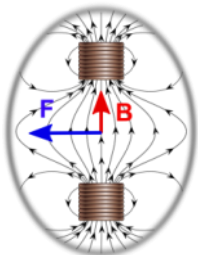
- ❶ accelerate the particles  
→ *radiofrequency cavities* :  $\vec{F} = q\vec{E}$
- ❷ deviate the particles (bend the trajectory)  
→ *dipolar magnets* :  $\vec{F} = q\vec{v} \wedge \vec{B}$
- ❸ focus the beam (concentrate the bunches)  
→ *quadripolar magnets*
- ❹ reduce aberrations  
→ *multipolar magnets*

The LHC today :

- ~ 1200 dipole magnets (L=14m)
- ~ 400 quadrupole magnets (L=3m)

The futur of LHC :

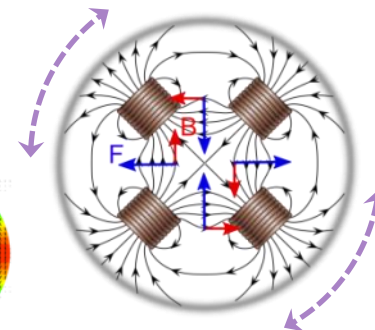
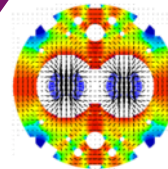
- HL-LHC (luminosity upgrade X 10) → 2022
- HE-LHC (energy upgrade X 2,5) → 2035



Dipoles are used to bend the beam trajectory

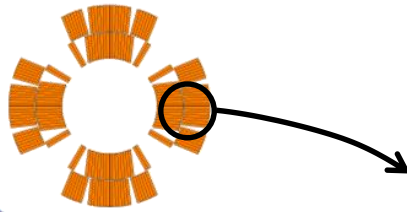
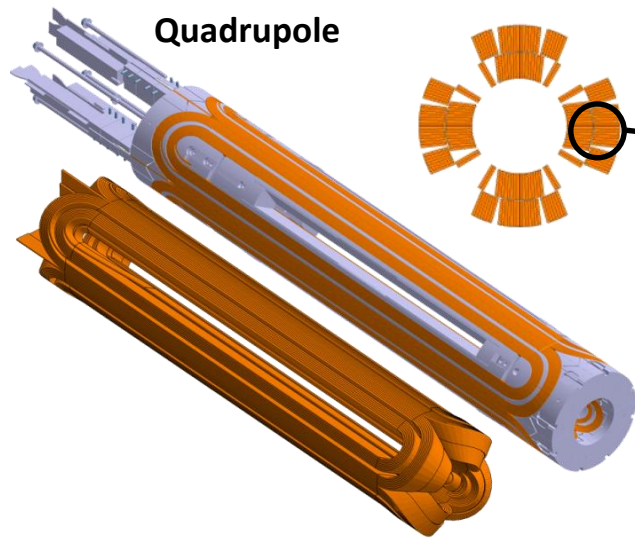


Increase  $\vec{B}$

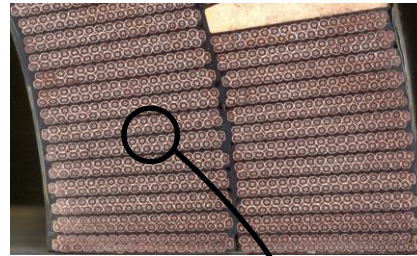


Quadrupoles are used for beam focusing

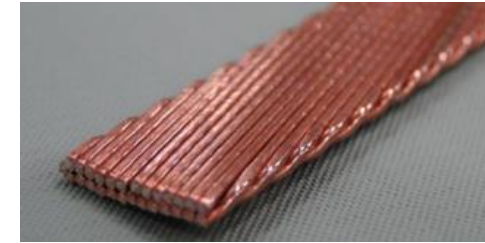




**Winding – stack ( $\approx$  m/cm )**



P. Ferracin, [www.uspas.fnal.gov](http://www.uspas.fnal.gov)  
Fermilab, <http://td.fnal.gov>  
G. Lenoir, PhD thesis



**Rutherford cable ( $\approx$  cm/mm )**



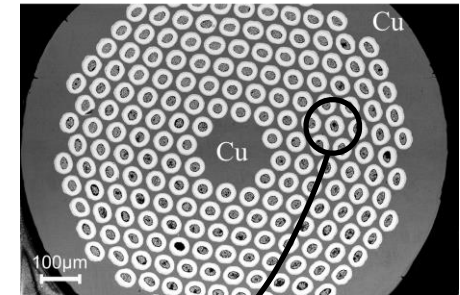
□ State of the art

- NbTi alloy currently used can reach 9/10T
- LHC's upgrade aims beyond 10 T

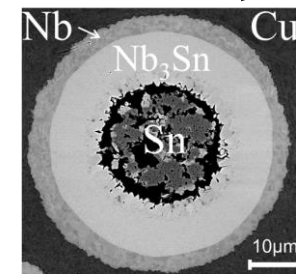
□ Development of Nb<sub>3</sub>Sn based conductor

- Complex manufacturing process
- Brittle material
- Electrical performances depends on mechanical state (strain)

**Strand ( $\approx$  mm/ $\mu$ m )**



- ➔ Influence of local phenomena **must be** understood  $\Rightarrow$  **relevant criterion**
- ➔ Superconductor behaviour should be anticipated  $\Rightarrow$  **predictive approach**
- ➔ Cable features should be optimized **mechanically**

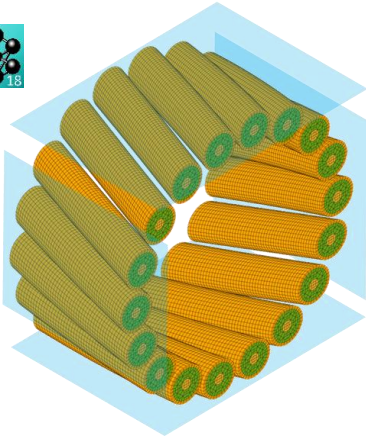
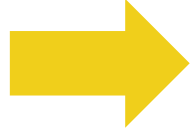


**FILAMENT ( $\approx$  mm/ $\mu$ m )**

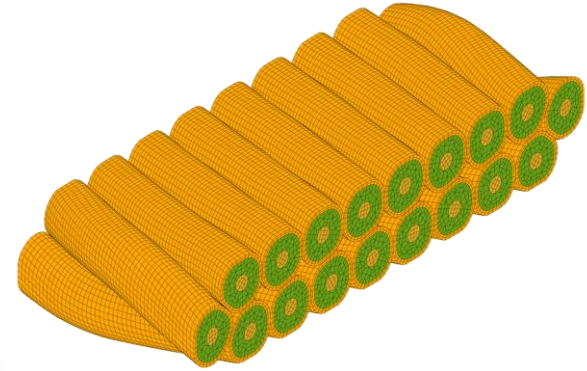
# OUTLINE

- GEOMETRIC MODEL (F. NUNIO)
  - ↳ Rutherford cables considering bi-metallic model
  - ↳ impregnation region
  - ↳ stack of conductors
  
- MECHANICAL MODEL (G. LENOIR)
  - ↳ Bi-metallic strand model based on RVE at the  $\mu$ -scale
  - ↳ Inverse identification of material parameters
  - ↳ Validation of the model

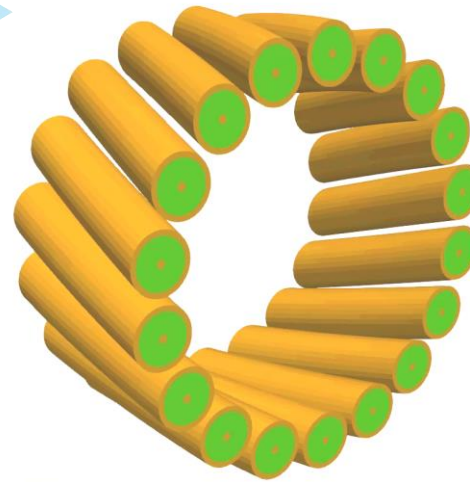
Initial model



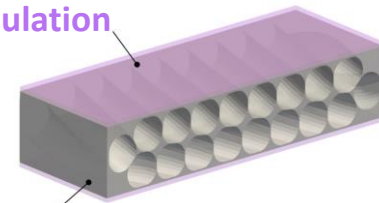
Cable compaction  
by 4 planes



Application of the displacement field

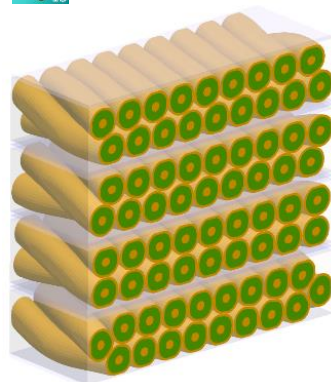
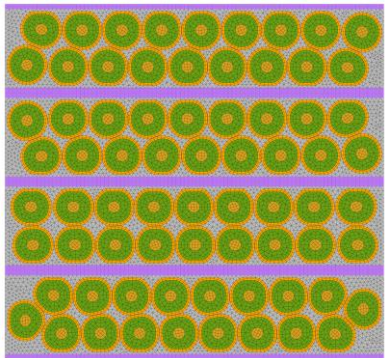


Impregnation  
insulation



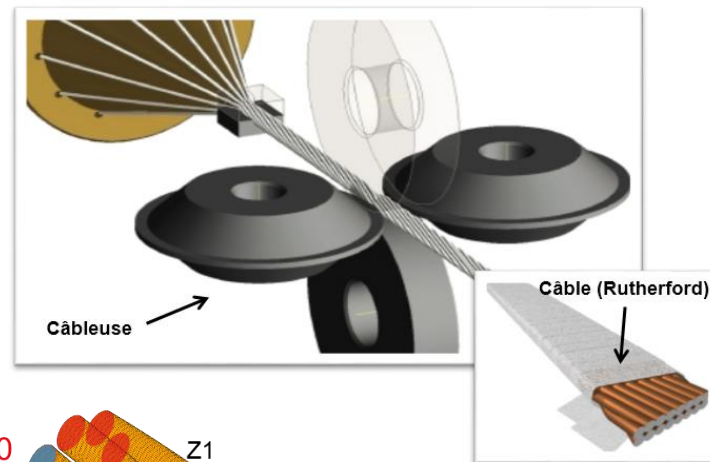
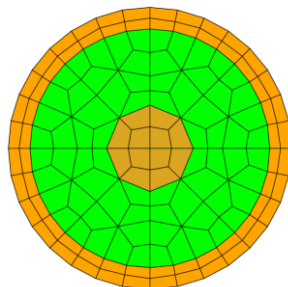
Epoxy matrix

Impregnation region

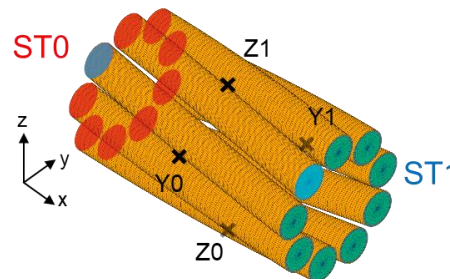


Stack of  
impregnated conductors

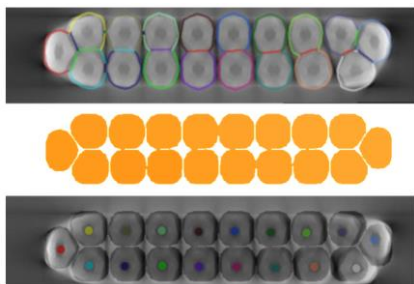
- Parametrization of the model :
  - ▣ Strand parameters
  - ▣ Cable parameters
    - Number of strands
    - Twist pitch P
    - Final size of the Rutherford shape W x H



- Benefits :
  - ▣ Cast3m script generates EPx input file
  - ▣ Persistence of the model's hierarchical structure during all modeling steps



⇒ **Adaptative tool for the prediction of the cable geometry**

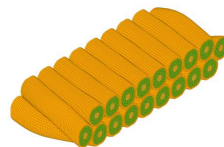


CT scan comparison

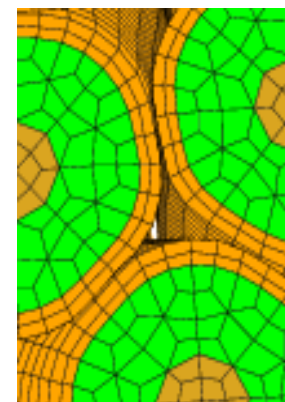
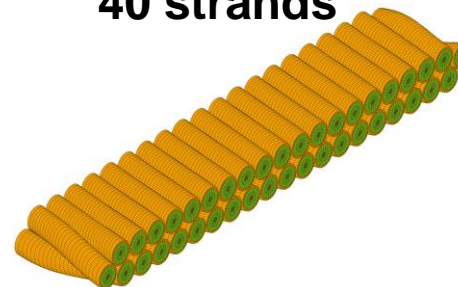
**9 strands**



**18 strands**

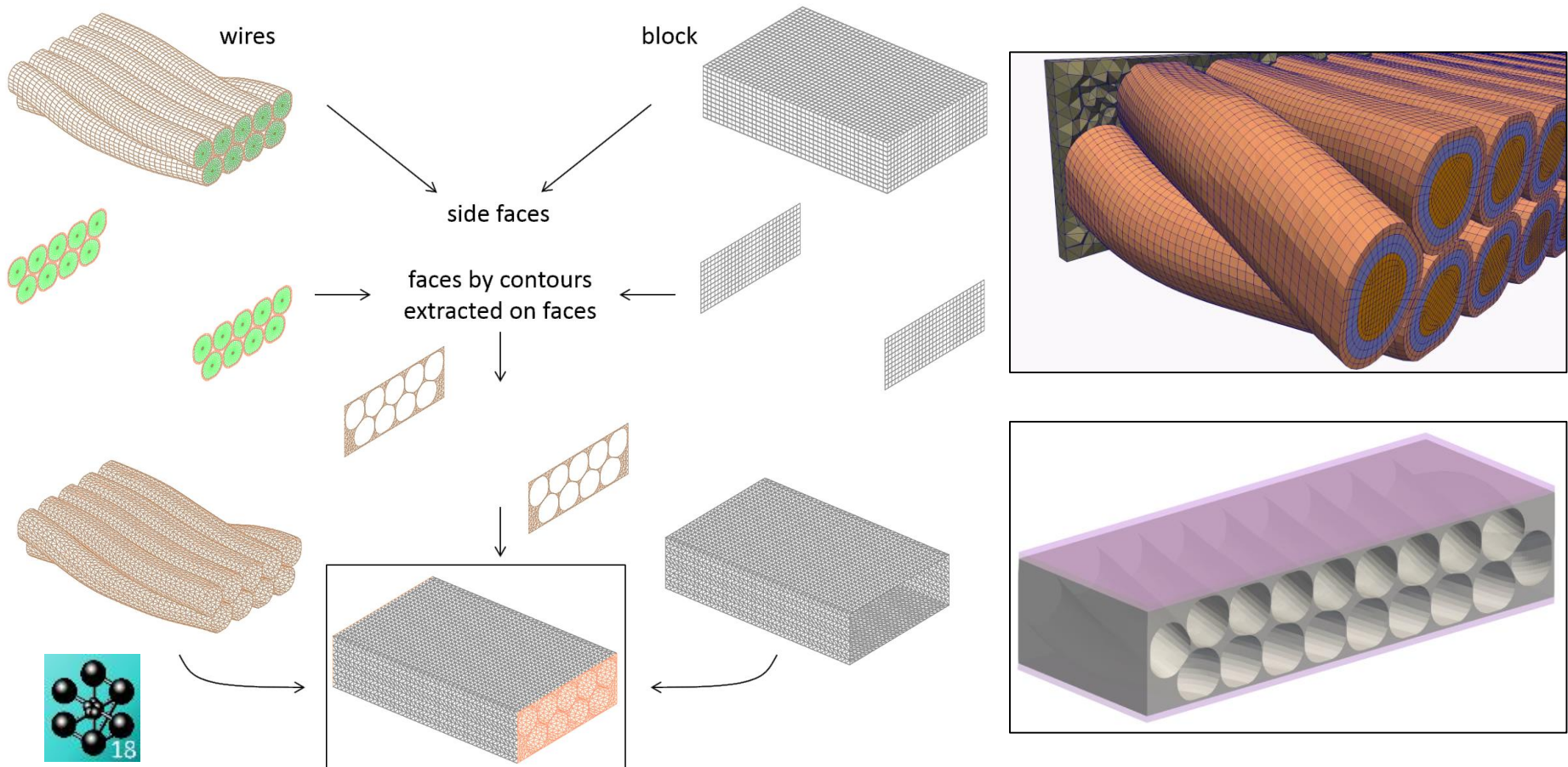


**40 strands**

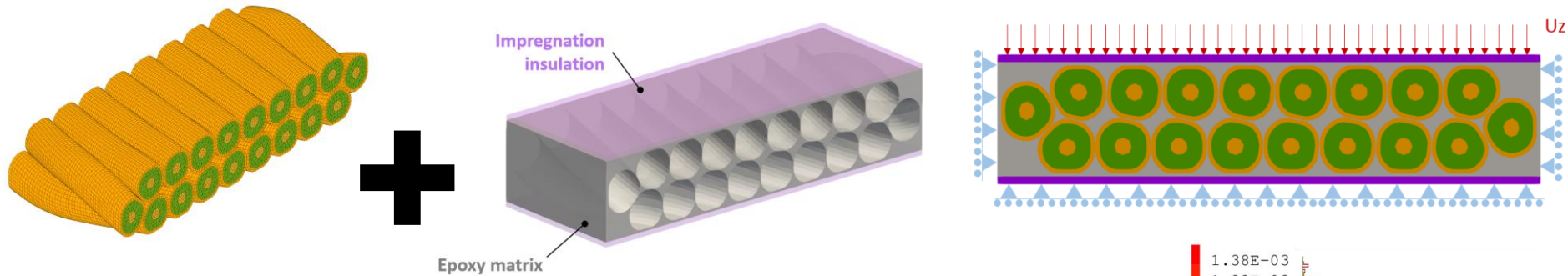


□ Matrix filler construction :

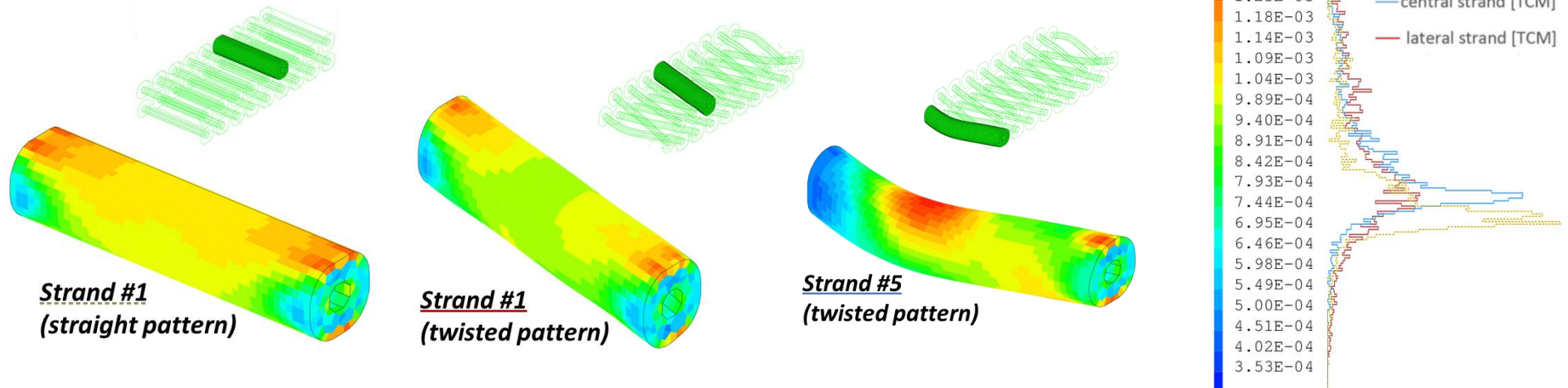
- ▣ not fully successful with reverse engineering methods (surface reconstruction, Boolean operators ...)
- ▣ no improvements with direct Boolean cut at the level of the mesh
- ▣ **method** : rebuild the skin of the matrix filler by a “sewing” technique, and mesh the volume



□ Model of impregnated Rutherford cable



□ Analysis of numerical compressive test on one stack




**⇒ Representative results of cable requires adapted mechanical model at the strand scale**  
*Bi-metallic model*



# OUTLINE

- GEOMETRIC MODEL (F. NUNIO)
  - ↳ Rutherford cables considering bi-metallic model
  - ↳ impregnation region
  - ↳ stack of conductors
  
- MECHANICAL MODEL (G. LENOIR)
  - ↳ Bi-metallic strand model based on RVE at the  $\mu$ -scale
  - ↳ Inverse identification of material parameters
  - ↳ Validation of the model

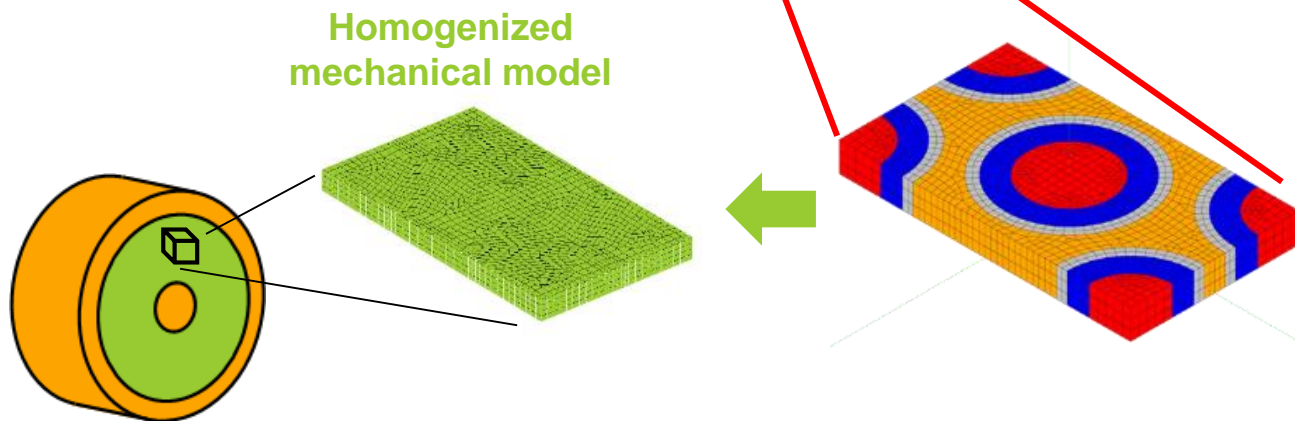
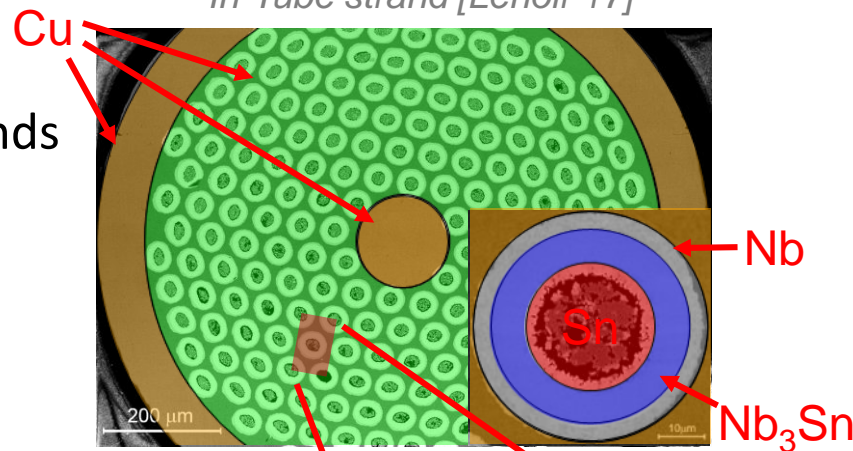
- Detailed mesh of strands in cable model numerically too expansive
  - ⇒ Simplified representation of the strands

- Filament scale Representative Volume Element (RVE)

- ▣ Interfilamentary matrix
- ▣ Superconducting phase
- ▣ Filament Barrier
- ▣ Filament Core

- Strand scale
  - ▣ Filamentary Region
  - ▣ Outer Layer
  - ▣ Strand Core

SEM transverse observation of a Powder-In-Tube strand [Lenoir 17]



⇒ Definition the composition of the bi-metallic model sets and their mechanical behavior

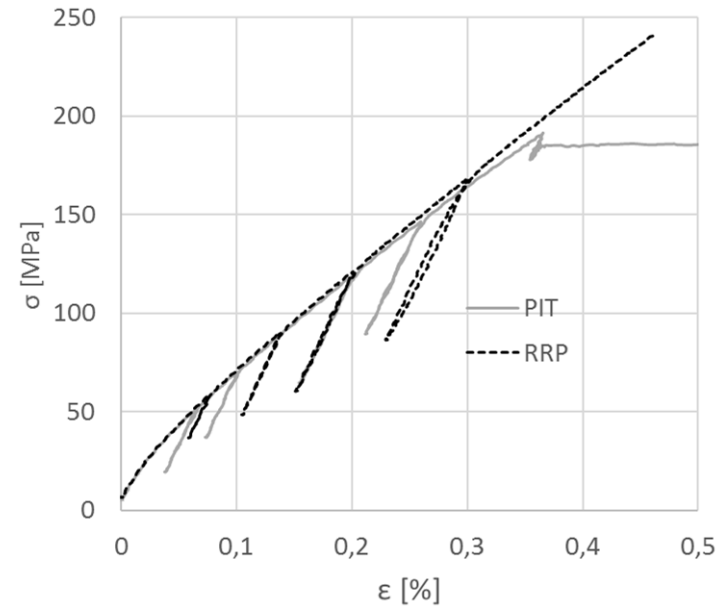
- Non-linear behavior of strands
  - ⇒ Adapted constitutive equation for elasto-plastic materials
  - ⇒ Predictability of non-monotonic behavior

□ Mechanical modeling [Lemaître 94]

- Von Mises yield criterion  $f(\sigma, X, R)$
- Elasticity with Hooke's law:  $\sigma = E * \varepsilon$
- Elasto-plasticity with hardening

[Armstrong 66] [Lemaître 94]

Isotropic:  $\dot{R} = b * (Q - R) * \dot{p}$       Hardening  
 Kinematic:  $\dot{X} = C * \varepsilon^p - \gamma * X * \dot{p}$       Plasticity  
Parameters

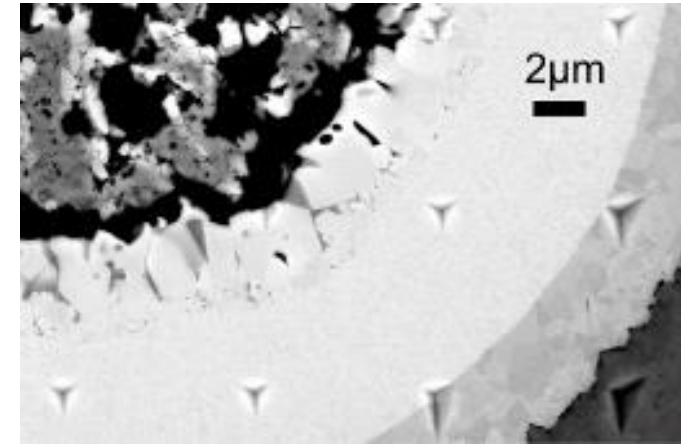
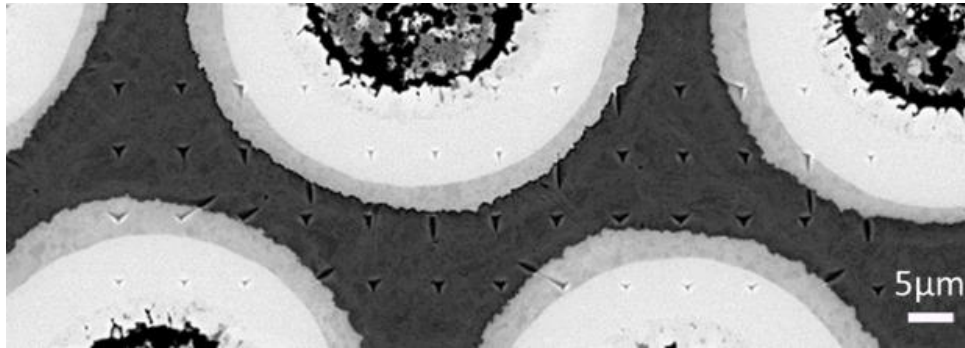


Tensile test on Nb<sub>3</sub>Sn strands [Lenoir 17]

➔ **3D-model based on internal variables of individual components**

[Lemaître 94] J. Lemaître and J.-L. Chaboche, U.K.: Cambridge Univ. Press, 1994.  
 [Armstrong 66] P.-J. Armstrong, C.-O. Frederick, Board Report, Berkeley Nuclear Laboratories, 1966.

## □ Observations



PIT	Indents number	E [GPa]	H [GPa]
Cu OL	18	133 ±5	1,25 ±0,08
Cu CO	15	125 ±4	1,14 ±0,07
Cu IF	92	132 ±6	1,33 ±0,13
Nb	13	125 ±13	1,69 ±0,43
Nb <sub>3</sub> Sn SG	35	171 ±6	13,1 ±0,56

## □ Results

- **Copper** considered as homogeneous
- **Niobium** behavior close to copper's
- **Nb<sub>3</sub>Sn**
  - Small grain phase purely elastic
  - Large grain phase not characterized
- **{Tin, porosities}** not characterized



## □ Composition & mechanical parameters

### ■ Strand Core, Outer-layer & Interfil. Matrix – Copper

⇒ Elasto-plastic with hardening -  $E_{Cu}, \nu_{Cu}, \sigma_{yCu}, b_{Cu}, Q_{Cu}, C_{Cu}, \gamma_{Cu}$

### ■ Supercond. – Nb<sub>3</sub>Sn

⇒ Elastic -  $E_{SC}, \nu_{SC}$

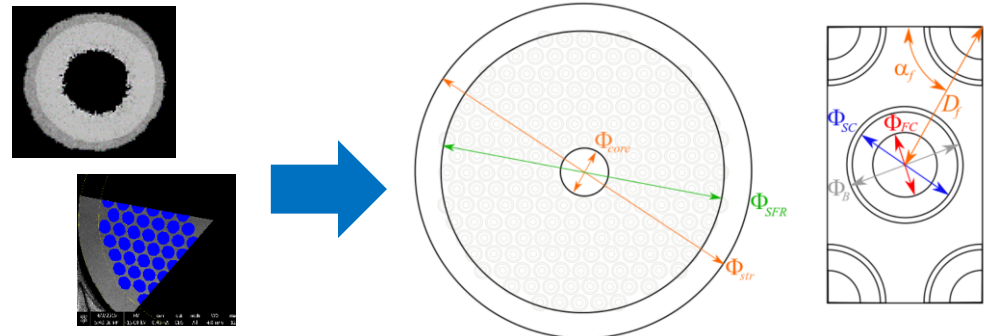
### ■ Filament Core - Sn / Porosities

⇒ Elastic -  $E_{FC}, \nu_{FC}$

## □ Geometrical parameters from Image analysis using ImageJ software

■ Strand:  $\emptyset_{str}, \emptyset_{SFR}, \emptyset_{core}$

■ RVE:  $\emptyset_{SC}, \emptyset_{FC}, D_f, \alpha_f$

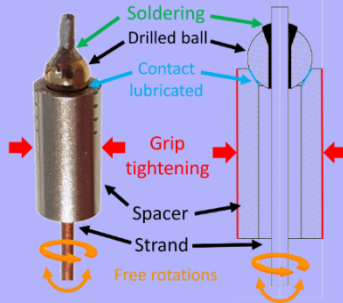
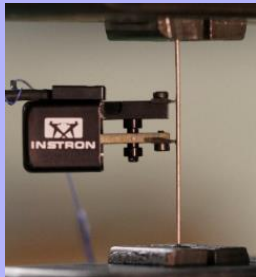
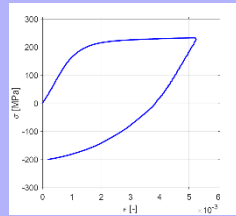


⇒ **Model parameters identify by direct measurements & inverse identification**

⇒ Finding the parameters which minimize the error between a model response and experimental data

## Tensile tests

- Performed at CEA
- SCUTT device [Lenoir 17]
- Room temperature
- Reacted strands



## Tensile tests model

- Parallel materials



- Homogeneous strain

$$\epsilon = \epsilon_{SC} = \epsilon_{FC} = \epsilon_{Cu}$$

- Stress distribution

$$\sigma = f_{vSC} * \sigma_{SC} + f_{vFC} * \sigma_{FC} + f_{vCu} * \sigma_{Cu}$$

- Behavior of the sets

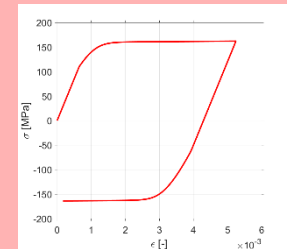
- Copper ⇒  $E_{Cu}, \nu_{Cu}$

$$\sigma_{yCu}, b_{Cu}, Q_{Cu}, C_{Cu}, \gamma_{Cu}$$

- Supercond ⇒  $E_{SC}, \nu_{SC}$

- Filament Core ⇒  $E_{FC}, \nu_{FC}$

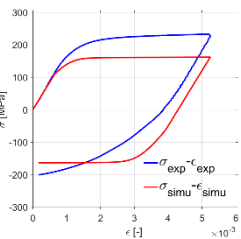
- Mech. differential system solved using a Runge-Kutta method



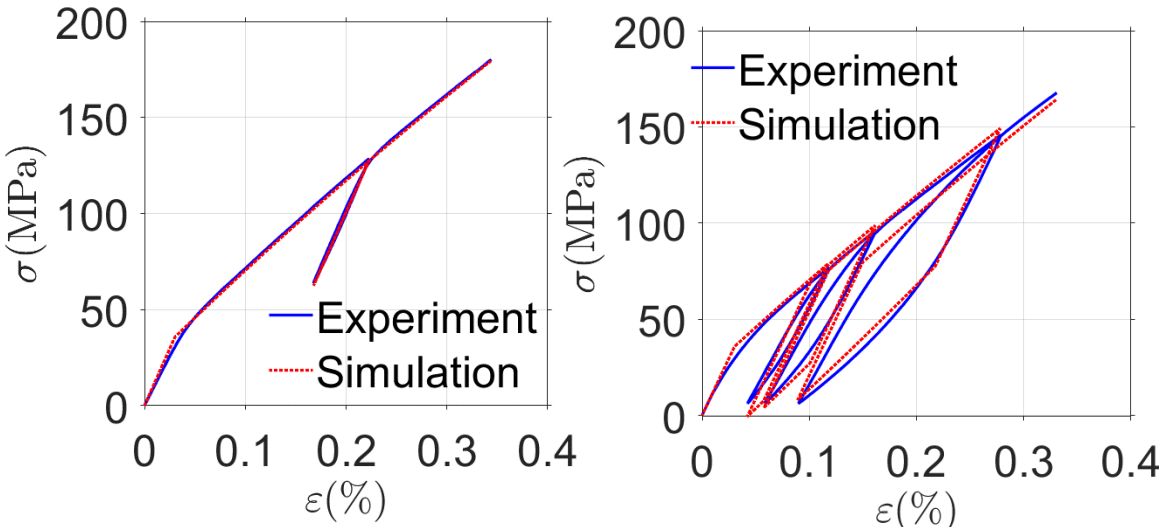
⇒ Optimization process

- Iteratively generate a set of parameters
- Compare the responses with a least square error
- Choose the set of parameters which minimize the error

Genetic & gradient-based algorithms



Comparison with the tensile tests used to identify the parameters



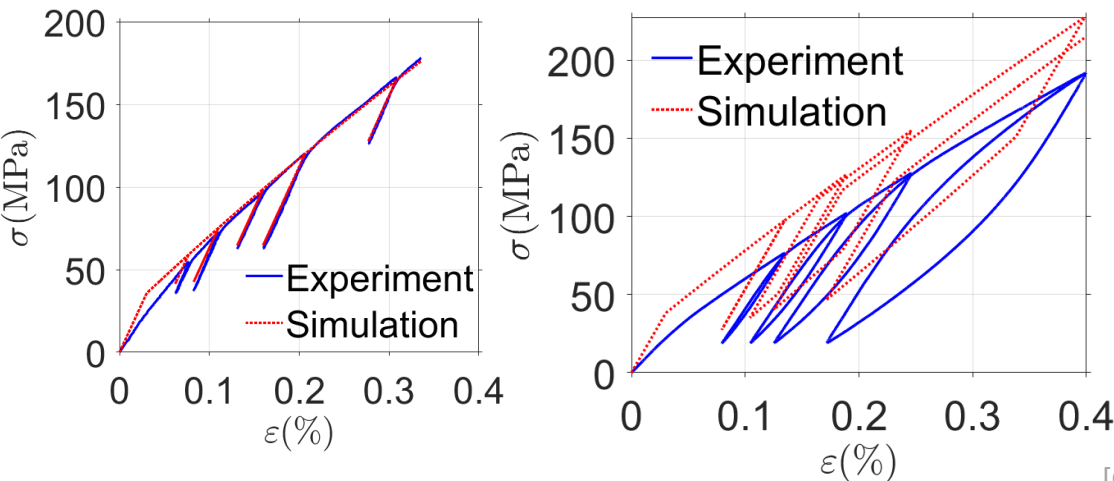
Fixed parameters

$$E_{Cu}, E_{SC}$$

Optimized parameters

$$E_{FC}, \sigma_{yCu}, C_{Cu}, \gamma_{Cu}$$

Comparison with independant tests



Comments

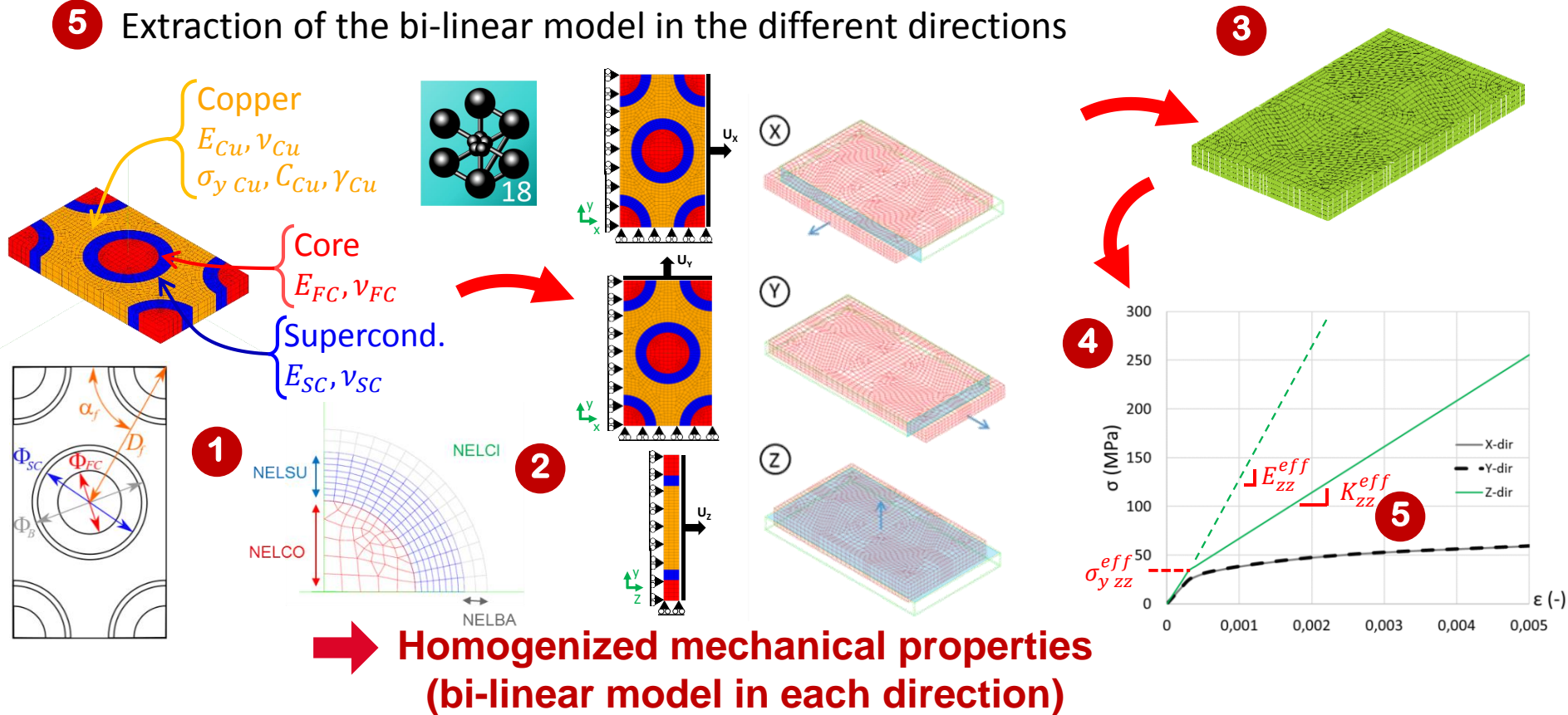
- Elastic moduli
- Loading plastic behavior
- Elasto-plastic unloading
- Initial slope / high  $\sigma_{yCu}$

Improvements

- Copper data
- Transverse tests on strand
- Adding kinematic hardening  
[Ohno 94]

[Ohno 94] N. Ohno & J.-D. Wang, *Eur. J. Mech. A/Solids*, 1994.

- 1 Definition of the geometry and the materials parameters from the identification process
- 2 Numerical tests in the different directions
- 3 Integration of stress and strain in the total volume
- 4 Plot of stress-strain curve in the total volume on the aimed direction
- 5 Extraction of the bi-linear model in the different directions





⇒ Comparison of the bi-metallic model response, detailed strand models & experimental data

□ Mechanical behavior

▣ Copper

↳ behavior laws from identification process

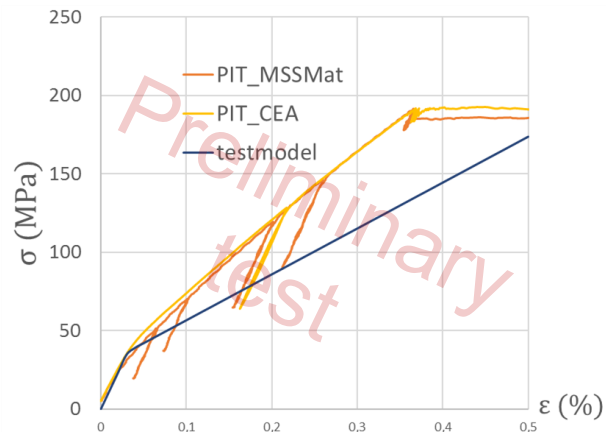
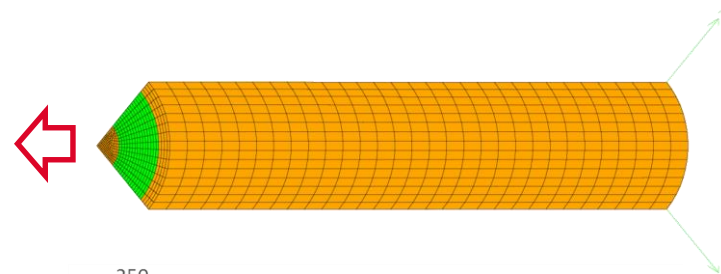
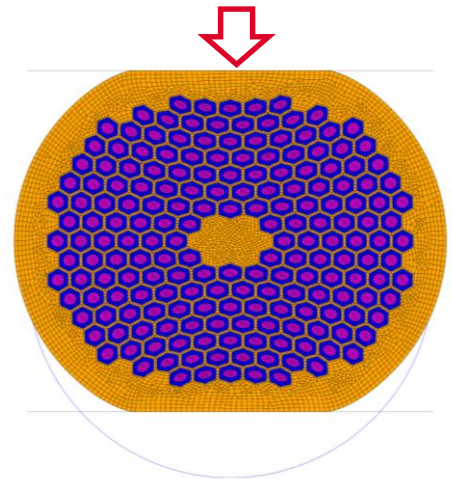
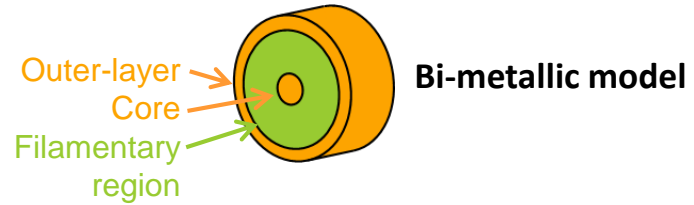
▣ Filamentary area

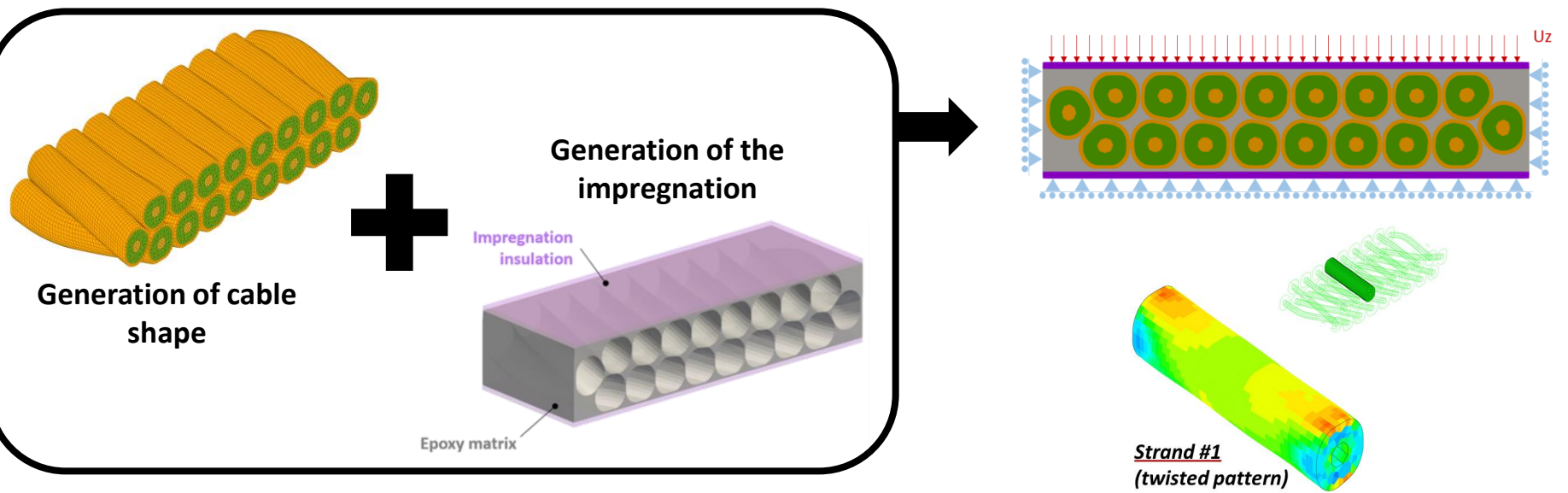
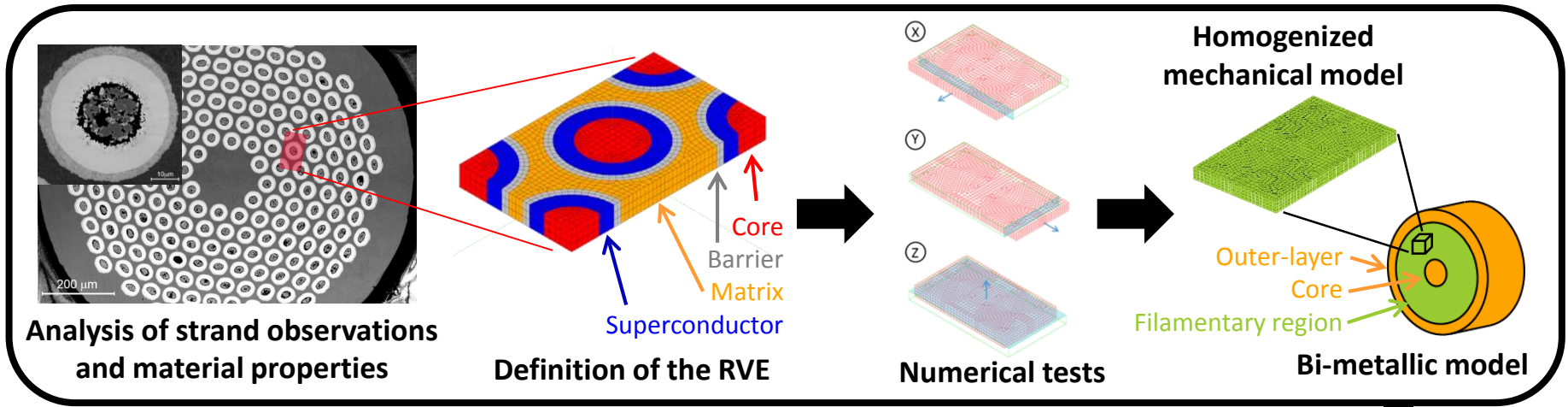
↳ bi-linear model from homogenization process

□ Numerical tests

▣ Transverse direction

▣ Tensile direction



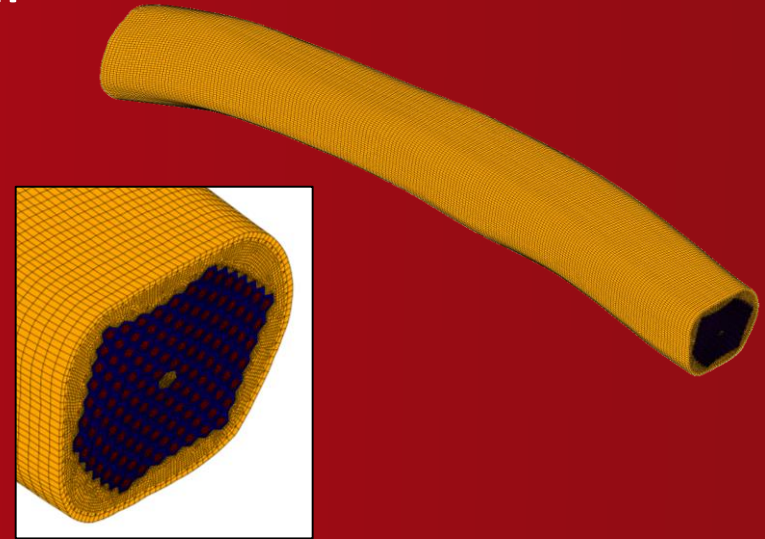
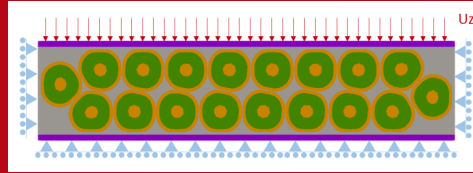


# SUMMARY

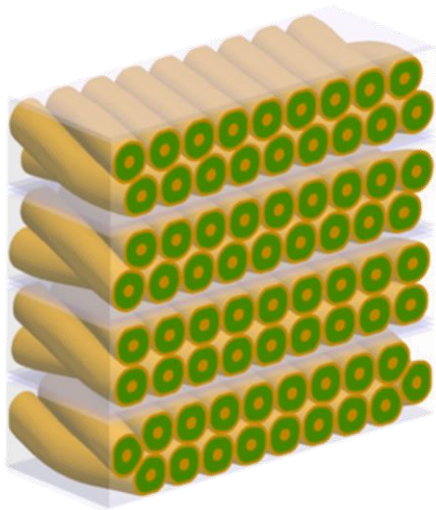
- GEOMETRIC MODEL
  - ↳ **Predictable** definition of the geometry of **Rutherford cables** considering **bi-metallic** model
  - ↳ **Robust and automated** creation of the **impregnation region**
  - ↳ Mechanical modelling of a **representative stack** of conductors
  
- MECHANICAL MODEL
  - ↳ **Bi-metallic strand model** based on **RVE at the  $\mu$ -scale**
  - ↳ Elasto-plastic behavior with **internal variables**
  - ↳ Can be used for **predictable modeling** of cables



- **Electrical prediction**

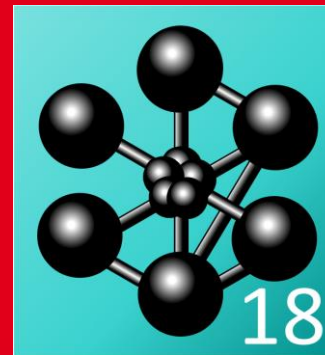


## PERSPECTIVES



- **Tensile tests at cryogenic temperature (on-going)**
- Nano-indentation at cryogenic temperature
- Enrichment of the experimental database with **transverse tests** and **copper data (on-going)**
- **Validation** of model prediction on experimental tests at **strand scale & cable (stack) scale**
- Add initial residual stress to account for strand heat treatment (experimental data needed)
- Improve the behavior law
- CoCaSCOPE platform

Gilles Lenoir  
@ gilles.lenoir@cea.fr  
R<sup>6</sup> Gilles\_Lenoir



**SPECIAL THANKS TO DEN/DM2S/SEMT/DYN  
(V. FAUCHER, O. JAMOND, T. LAPORTE)**

Analyse multi-échelle de câbles  
supraconducteurs

G. Lenoir, P. Manil, F. Nunio

CEA Paris-Saclay – IRFU, Université Paris-Saclay

Commissariat à l'énergie atomique et aux énergies alternatives  
Centre de Saclay | 91191 Gif-sur-Yvette Cedex, FRANCE  
Direction de la Recherche Fondamentale  
Institut de recherche sur les lois fondamentales de l'Univers  
Département d'Ingénierie des Systèmes  
Laboratoire de Conception, d'études et d'Avant-Projets

Etablissement public à caractère industriel et commercial | R.C.S Paris B 775 685 019



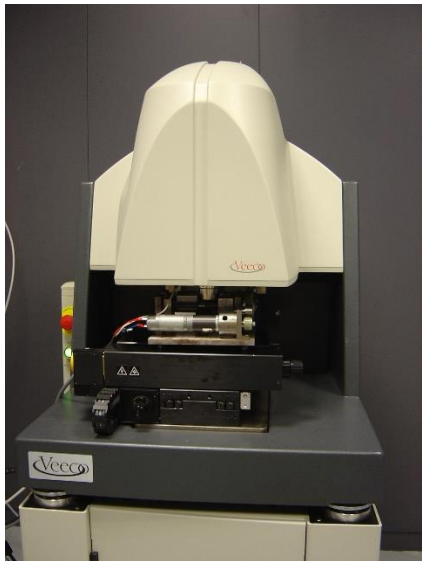


Material	E (GPa)	Reference	$E_{\text{Nano-ind.}}$
Copper	80	[Bajas 11]	129GPa
	108	[Scheuerlein 17]	
	116	[Alknes 16]	
	118	[Sugano 16]	
	128-137	[Mitchell 05]	
Nb <sub>3</sub> Sn	124	[Dylla 16]	171GPa
	127	[Hojo 06]	
	132	[Bussiere 80]	
	135-100	[Mitchell 05]	
	136	[Scheuerlein 15]	
	137	[Keller 67]	
	144	[Poirier 84]	
	150-65	[Bray 97]	
	165	[Easton 80]	
179-168	[West 79]		
Niobium	92	[Alknes 16]	125GPa
	103	[Sugano 15]	
	105-110	[Mitchell 05]	

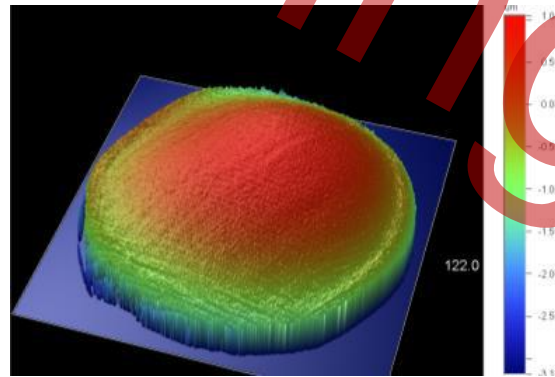
- Differences in
  - ▣ Manufacturing process
    - Of materials
    - Of strands
  - ▣ Measured object
    - Complete strand
    - Filaments bundles (w/o matrix)
    - Single filament
    - Tapes (ex: Nb<sub>3</sub>Sn layers/ductile substrate)
    - Single cristal
  - ▣ Measurement methods
    - Axial extensometer and load cell
    - Optical extensometer
    - Resonant Ultrasound Spectroscopy
    - Cristallographic orientation
  - ▣ Direct measurement vs Mixture laws
- Based on literature values  
( $E_{\text{Nb}}$ , single cristal properties, ASM International)



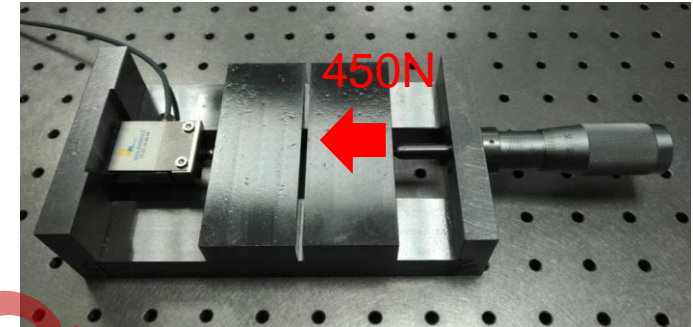
- Collaboration with ENSAM Châlons  
(R. Rotinat, R. Moulart, L. Fouilland, C. Person)
  - ▣ Digital Image Correlation during an *in-situ* transversal compression test
  - ▣ Objective
    - Quantify anisotropy
    - Include additional data for behavior laws identification



Compression device inside the interferometric microscope



Planarity analysis of a copper wire and a strand



Compression device

